

EE-3221 - Dr. Durant - Quiz 6
Winter 2020-'21, Week 7

This is an **open**-book quiz. You may use a calculator. You may refer to your homework that is due today.

Find the inverse z-transform of $X(z) = \frac{-z}{z^2 + 0.2z - 0.24}$

Solve for poles (roots of denominator):

$$z^2 + 0.2z - 0.24 = 0$$

$$z = \frac{-0.2 \pm \sqrt{0.04 + 0.96}}{2} = \frac{-0.2 \pm 1}{2} = -0.6, +0.4$$

$$\begin{aligned} \frac{X(z)}{z} &= \frac{-1}{z^2 + 0.2z - 0.24} = \frac{A}{z + 0.6} + \frac{B}{z - 0.4} \\ -1 &= A(z - 0.4) + B(z + 0.6) \\ -1 &= (A+B)z + (0.4A + 0.6B) \end{aligned}$$

$$\begin{aligned} A+B &= 0 \\ 0.4A + 0.6B &= -1 \\ 0.4B + 0.6B &= -1 \\ B &= -1 \rightarrow A = 1 \end{aligned}$$

$$X(z) = \frac{z}{z + 0.6} - \frac{z}{z - 0.4}$$

$$x(n) = ((-0.6)^n - (0.4)^n) u(n)$$