

**EE-3220 - Dr. Durant - Quiz 3**  
**Winter 2016-'17, Week 3**

1. (3 points) Calculate the convolution  $y(n) = x_2(n) * h_2(n) = [3 \ 6 \ -1] * [2 \ -5 \ 4]$ . Show your work (intermediate products; you are not required to show the formula for the convolution sum). Both sequences start at  $n=0$ .

	$n$				
$k$	0	1	2	3	4
0	6	-15	12		
1		12	-30	24	
2			-2	5	-4
	—	—	—	—	—
$y:$	6	-3	-20	29	-4

$$y(n) = \sum_{k=-\infty}^{\infty} x(k) h(n-k)$$

2. (3 points) **Calculate** the first 4 samples of the unit **impulse** response of  $y(n) = 3y(n-1) + 2x(n) - 5x(n-1)$ . Recall that the impulse response is  $y(n)$  when  $x(n) = \delta(n)$ .
3. (2 points) **Re-write** the equation in standard form. **Indicate** the name of each coefficient ( $a_1$ , etc.).
4. (2 points) **Write MATLAB code** using `filter(b,a,x)` function in MATLAB that calculates the first 10 samples of the unit **impulse** response,  $h$ . Write the complete code needed to calculate  $h$ .

$n$	$x(n)$	$y(n)$
0	1	$3y(-1) + 2x(0) - 5x(-1) = 3 \cdot 0 + 2 \cdot 1 - 5 \cdot 0 = 0 + 2 - 0 = 2$
1	0	$3y(0) + 2x(1) - 5x(0) = 3 \cdot 2 + 2 \cdot 0 - 5 \cdot 1 = 6 + 0 - 5 = 1$
2	0	$3y(1) + 2x(2) - 5x(1) = 3 \cdot 1 + 2 \cdot 0 - 5 \cdot 0 = 3 + 0 - 0 = 3$
3	0	$3y(2) + 2x(3) - 5x(2) = 3 \cdot 3 + 2 \cdot 0 - 5 \cdot 0 = 9 + 0 - 0 = 9$

$$\textcircled{3} \quad \underset{\substack{\uparrow \\ a_0}}{y(n)} - \underset{\substack{\uparrow \\ a_1}}{3y(n-1)} = \underset{\substack{\uparrow \\ b_0}}{2x(n)} - \underset{\substack{\uparrow \\ b_1}}{5x(n-1)}$$

$$\textcircled{4} \quad a = [1 \quad -3];$$

$$b = [2 \quad -5];$$

$$n = 0:10;$$

$$d = n == 0; \quad \% x(n) = \delta(n)$$

$$h = \text{filter}(b, a, d); \quad \% h(n) = y(n) \text{ when } x(n) = \delta(n)$$

% Dr. Durant - EE3220 Quiz 3 - 2016-12-13

figure

%% Problem 1

x2 = [3 6 -1];

h2 = [2 -5 4];

y = conv(x2,h2); % result: [6 -3 -20 29 -4]

n1 = 0:(length(y)-1);

subplot(2,1,1), stem(n1,y), title('Problem 1')

%% Problem 4

a = [1 -3];

b = [2 -5];

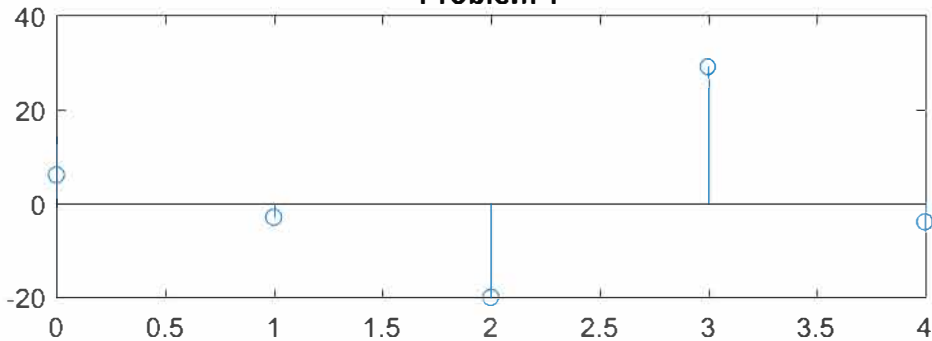
n = 0:10;

d = n == 0; % x(n) = delta(n)

h = filter(b,a,d); % h(n) = y(n) when x(n) = delta(n)

% result = [2 1 3 9 27 81 243 729 2187 6561 19683] (unstable!)

subplot(2,1,2), stem(n,h), title('Problem 4')

**Problem 1****Problem 4**