

EE-3220-11 – Dr. Durant – Quiz 3
Winter 2015-'16, Week 3

1. (2 points) **Calculate** the first 4 samples of the unit **impulse** response of $y(n) = 0.8 y(n-1) + x(n) - 2x(n-1) + 3x(n-2)$. Recall that the impulse response is $y(n)$ when $x(n) = \delta(n)$.
 - $y(0) = 0.8 y(-1) + x(0) - 2x(-1) + 3x(-2) = 0.8 \times 0 + 1 - 2 \times 0 + 3 \times 0 = 1$
 - $y(1) = 0.8 y(0) + x(1) - 2x(0) + 3x(-1) = 0.8 \times 1 + 0 - 2 \times 1 + 3 \times 0 = -1.2$
 - $y(2) = 0.8 y(1) + x(2) - 2x(1) + 3x(0) = 0.8 \times -1.2 + 0 - 2 \times 0 + 3 \times 1 = 2.04$
 - $y(3) = 0.8 y(2) + x(3) - 2x(2) + 3x(1) = 0.8 \times 2.04 + 0 - 2 \times 0 + 3 \times 0 = 1.632$

2. (2 points) **Calculate** the first 4 samples of the unit **step** response of the above difference equation. Recall that the step response is $y(n)$ when $x(n) = u(n)$.
 - $y(0) = 0.8 y(-1) + x(0) - 2x(-1) + 3x(-2) = 0.8 \times 0 + 1 - 2 \times 0 + 3 \times 0 = 1$
 - $y(1) = 0.8 y(0) + x(1) - 2x(0) + 3x(-1) = 0.8 \times 1 + 1 - 2 \times 1 + 3 \times 0 = -0.2$
 - $y(2) = 0.8 y(1) + x(2) - 2x(1) + 3x(0) = 0.8 \times -0.2 + 1 - 2 \times 1 + 3 \times 1 = 1.84$
 - $y(3) = 0.8 y(2) + x(3) - 2x(2) + 3x(1) = 0.8 \times 1.84 + 1 - 2 \times 1 + 3 \times 1 = 3.472$

3. (2 points) **Re-write** the equation in standard form. **Indicate** the name of each coefficient (a_1 , etc.).
 - $y(n) - 0.8 y(n-1) = x(n) - 2x(n-1) + 3x(n-2)$
 - $a_0 y(n) + a_1 y(n-1) = b_0 x(n) + b_1 x(n-1) + b_2 x(n-2)$

4. (2 points) What is the vector of “a” or autoregressive or IIR (infinite impulse response) coefficients in the above equation? (Recall that the “b” or FIR coefficients correspond to a weighted sum of inputs.)
 - $a = [1 \ -0.8]$

5. (2 points) **Write MATLAB code** using filter function in MATLAB that calculates the first 10 samples of the unit **impulse** response, h . Write the complete code needed to calculate h .
 - $h = \text{filter}([1 \ -2 \ 3], [1 \ -0.8], [1 \ \text{zeros}(1,9)]);$

Checking results in MATLAB:

```
a = [1 -0.8]; % move a1 to left side for standard form  
b = [1 -2 3];
```

```
% Problem 1  
y1 = filter(b,a,[1 0 0 0])
```

```
% Problem 2  
y2 = filter(b,a,ones(1,4))
```

```
% Problem 5  
h = filter([1 -2 3], [1 -0.8], [1 zeros(1,9)])
```

```
%{  
Output  
quiz3  
y1 =  
    1.0000    -1.2000    2.0400    1.6320  
y2 =  
    1.0000    -0.2000    1.8400    3.4720  
h =  
Columns 1 through 9  
    1.0000    -1.2000    2.0400    1.6320    1.3056    1.0445    0.8356    0.6685    0.5348  
Column 10  
    0.4278  
%}
```