

EE-3220-11 - Dr. Durant - Quiz 2
Spring 2015, Week 2

1. (3 points) Indicate whether each of the following systems is linear, time-invariant, and causal. You **do not** need to show your work for this problem.

	$y_1(n) = x(n-3)$	$y_2(n) = x(n+2)$	$y_3(n) = nx^2(n-1)$
Linear?	+	+	-
Time-invariant?	+	+	-
Causal?	+	-	+

2. (2 points) Write the non-0 portion of the sequence resulting from $x(n) = (\frac{1}{2})^{-n} (u(n+2) - u(n-2))$. Recall that $u(n)$ is the unit step that becomes 1 when the argument reaches 0. Clearly indicate the $n=0$ position in your sequence. (off by 1)
3. (2 points) Express your sequence above as a weighted sum of shifted unit samples or deltas ($\delta(\cdot)$).
4. (1 point) Let the impulse response of a system be $h(n) = [h(-1) \ h(0) \ h(1)] = [6 \ 3 \ 1]$. Explain why this system is not causal.
5. (2 points) Calculate the convolution $y(n) = x_1(n) * h_2(n) = [5 \ -3 \ 2] * [7 \ 5 \ 2]$. Show your work (intermediate products; you are not required to show the formula for the convolution sum). Both sequences start at $n=0$. Indicate where $n=0$ in your result

② $u(n+2) - u(n-2) = [1 \ 1 \ 1 \ 1]$ (note: value of 0 @ $n=2$)
 so, effectively, $n = -2:1$ for non-zero values of x
 $x = (\frac{1}{2})^{-n} [2 \ -1 \ 0 \ 1] = 2^{n+2} [-2 \ -1 \ 0 \ 1] = [\frac{1}{4} \ \frac{1}{2} \ 1 \ 2]$

③ $x(n) = \frac{1}{4}\delta(n+2) + \frac{1}{2}\delta(n+1) + \delta(n) + 2\delta(n-1)$

④ $h(-1) \neq 0 \rightarrow$ output occurs before input

⑤ if false

⑤ Convolution table:

$x(n)$	0	1	2				
	5	-3	2				
		7	5	2			
			-21	-15	-6		
				14	10	4	

$y(n) = [\frac{35}{4} \ \frac{1}{4} \ \frac{9}{4} \ \frac{1}{4} \ \frac{4}{4}]$