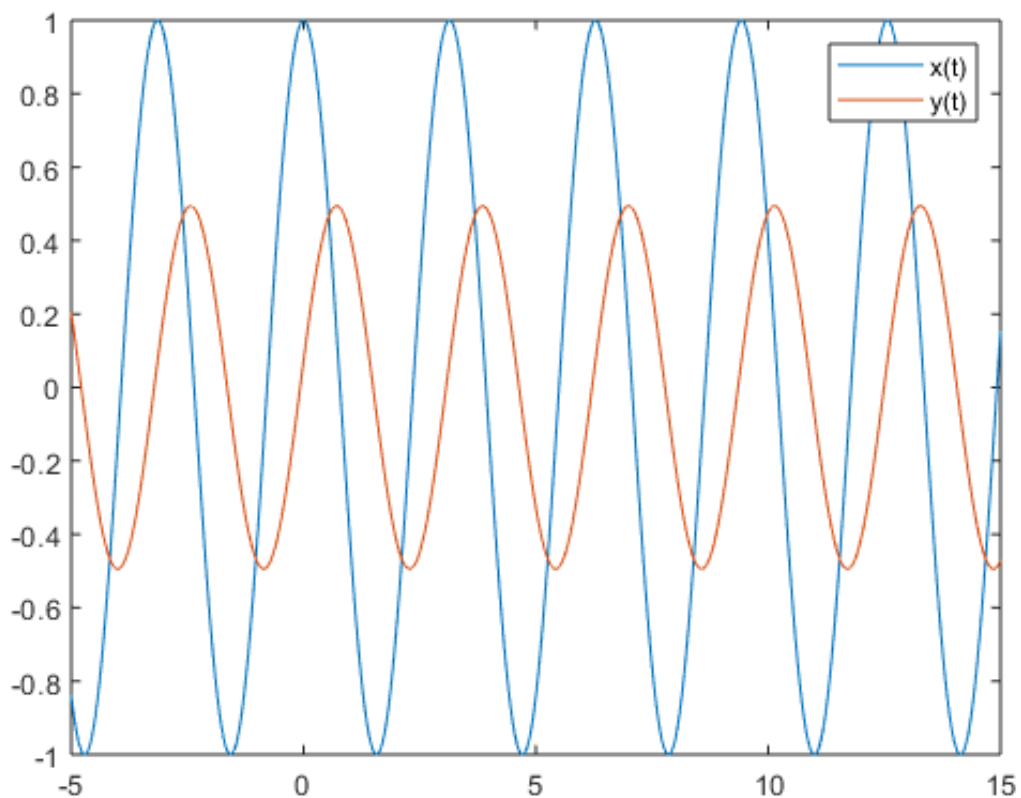


EE3032-4, W5D4 example, Transfer function applied to a sinusoid.

```
w = 2; % omega, radians/s
a = 0.3; % decay coefficient, 1/s (Hz)
t = linspace(-5,15,1000);
x = cos(w*t); % input function
```

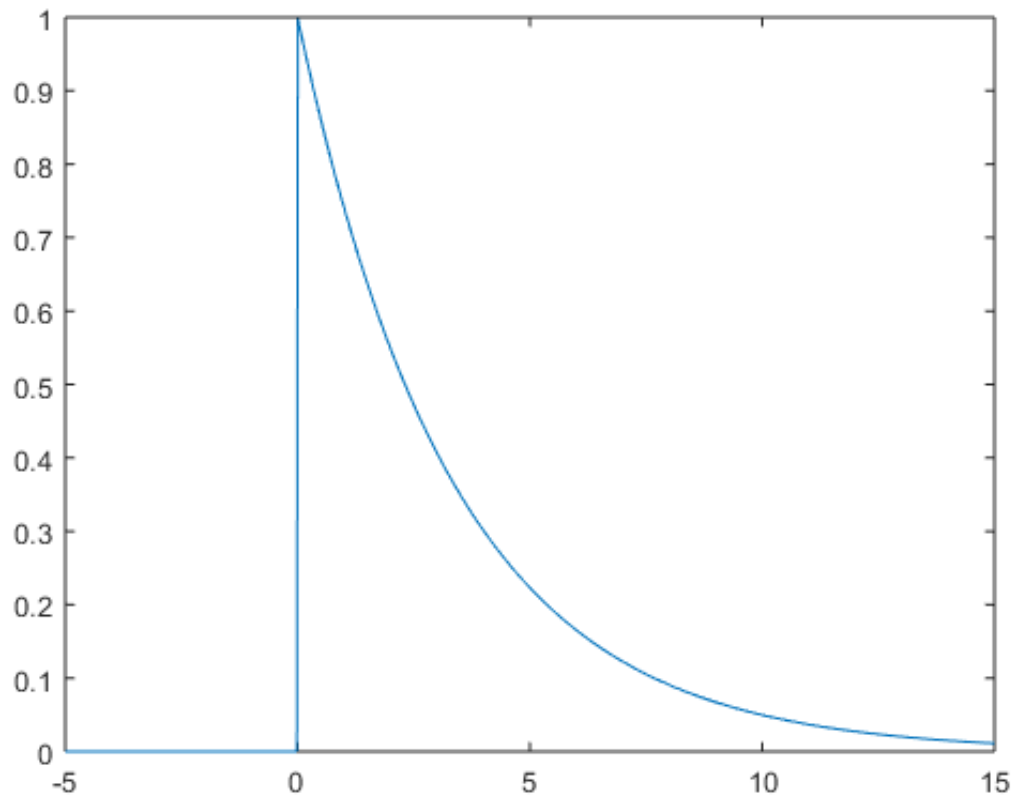
We derived the following expression for $H(\omega)$ in class.

```
H = 1 / (a + 1j * w); % H(w)
y = abs(H) * cos(w*t + angle(H)); % transfer function theory
plot(t,x, t,y), legend('x(t)', 'y(t)')
```

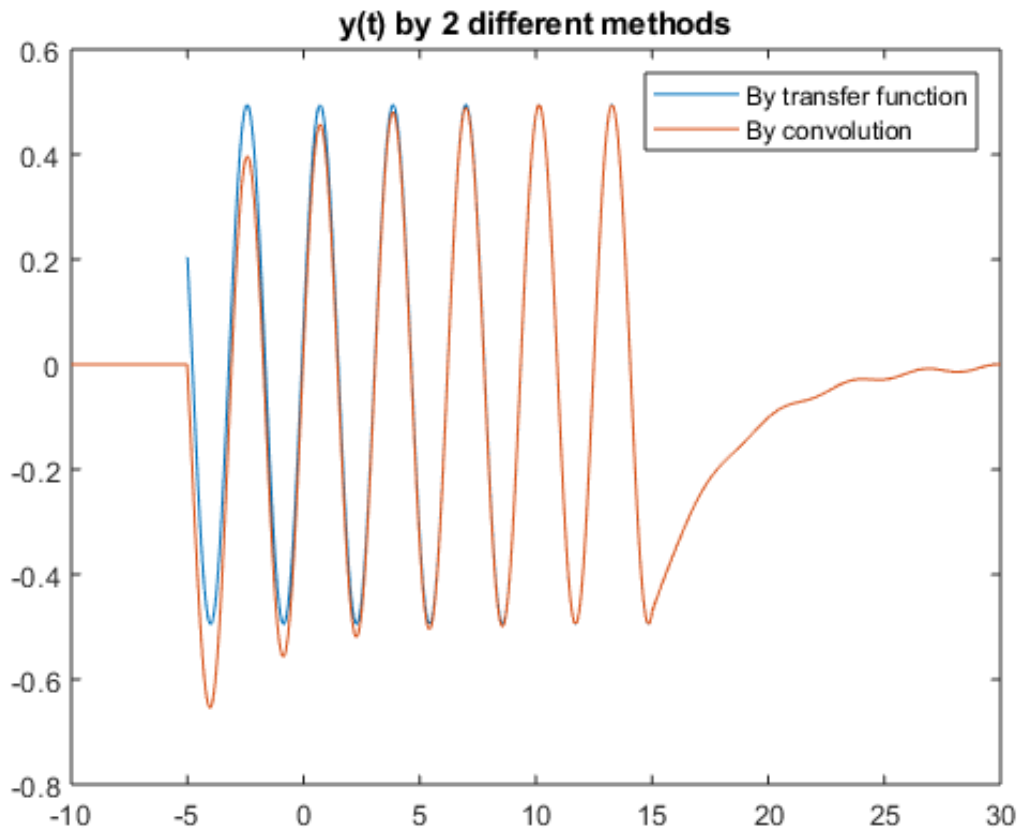


Now, let's calculate the system output using another method, convolution directly.

```
h = exp(-a*t) .* (t>0);
plot(t,h)
```



```
dt = diff(t(1:2));  
y2 = conv(x,h)*dt; % Riemann convolution integral  
ty2 = linspace(2*t(1), 2*t(end), length(t)*2-1); % width property  
plot(t,y, ty2,y2)  
title('y(t) by 2 different methods')  
legend('By transfer function', 'By convolution')
```



These approaches agree in the central portion. Note that convolution diverges from the correct result at the edge. The main reason for this is that the input $x(t)$ is implicitly taken as 0 outside the range where it is defined (t values). Additionally, there is some error since the right tail of $h(t)$ is truncated.