Name Answels

EE3032 - Dr. Durant - Quiz 8 Winter 2019-'20, Week 9

Convolution integral: $y(t) = \int_{-\infty}^{\infty} x(\tau)h(t-\tau)d\tau$ Transfer function: $H(\omega) = \int_{-\infty}^{\infty} h(t)e^{-j\omega t}dt$

Fourier series (periodic fcn.): $x(t) = \sum_{n=-\infty}^{\infty} X_n e^{jn\omega_0 t} = a_0 + 2\sum_{n=1}^{\infty} \alpha_n \cos(n\omega_0 t) - \beta_n \sin(n\omega_0 t)$

 $\alpha \& \beta$ are the real & imaginary parts of X (not a & b, which are the coefficients in the trig. form).

A real, periodic signal's Fourier Series terms include $X_0 = 0$, $X_1 = 3$ and $X_2 = 5$ -j7. $X_n = 0$ for n > 2.

- 1. (2 points) List all the other non-0 terms of X and their values.
- 2. (2 points) Calculate the power using Parseval's theorem, which states that the power is the sum of the squared magnitudes of **all** the Fourier Series coefficients. Show your work.
- 3. (2 points) Does the signal have even symmetry, odd symmetry, or neither? Explain your answer.
- 4. (2 points) Calculate the exponential term in the Fourier series associated with X₁. (Leave it in exponential form; in general, this will have a complex value.)
- 5. (1 point) Calculate a₁ and b₁ by converting X₁ accordingly. Recall that the trigonometric coefficients include the amplitude contributions from the positive *and* negative frequencies and are the coefficients of the appropriate cosine and sine terms.
- 6. (1 point) State the trigonometric terms in the signal due to a_1 and b_1 with correct amplitude, phase, and frequency.

$$\begin{array}{l} (2) \times_{-1} = \chi_{1}^{*} = 3 \\ \times_{-2} = \chi_{1}^{*} = 5 + i 7 \\ (3) P = \frac{2}{5} \times_{n} \chi_{n}^{*} = \chi_{0}^{2} + 2(\chi_{1} \times i^{*} + \chi_{2} \times j^{*}) \\ = 0 + 2(9 + 25 + 49) = 166 \\ (3) N_{0} i \gamma h_{0} r. \times_{2} is \ complex: \ beth \ cos/sin \ (evon \ radd) \ parts. \\ (3) N_{0} i \gamma h_{0} r. \times_{2} is \ complex: \ beth \ cos/sin \ (evon \ radd) \ parts. \\ (5) \times_{i} i^{lobt} = 3 e^{i mot} \\ (5) From \ given \ F.5. : \ a_{n} = 2\alpha_{n} = 2\Omega_{0}(\chi_{n}), \ b_{n} = -2\beta_{n} = -2\beta_{m}(\chi_{n}), \ n \ge a_{1} = 2 \cdot 3 = 6 \quad b_{i} = -2 \cdot 0 = 0 \\ (6) \ a_{1} cos(nu_{0}t) + b_{1} sin(n + b_{1}t) = 6 \cos(\omega_{0}t) \\ lote: \ 6) = 2 \cdot \Omega_{0}(4) \\ \end{array}$$