

Milwaukee School of Engineering
Electrical Engineering and Computer Science Department

EE-3032 – Practice Final Exam –
Dr. Durant

November, 2019

May use 8½" × 11" note sheet. No calculator.
Tables 5.6 and 5.7 from Dr. Yagle's text will be provided.

Good luck!

Name: _____

Page 3: (17 points) _____

Page 4: (24 points) _____

Page 5: (16 points) _____

Page 6: (15 points) _____

Page 7: (12 points) _____

Page 8: (16 points) _____

Total: (100 points) _____

1. (4 points) **Sketch** $x(t) = r(t+2) - u(t-1) + \delta(t-2)$
2. (4 points) **Explain** whether $s(t) = 4 + \sin(4\pi t) + \cos(9\pi t)$ is **periodic**. If it is, calculate its **fundamental period**.
3. (5 points) **Calculate** $S(\omega)$, the Fourier transform of $y(t)$, or explain why it cannot be done.
4. (4 points) **Explain** whether $y(t) = \cos(t) + \sin(t\sqrt{3})$ is **periodic**. If it is, calculate its **fundamental period**.

5. (3 points) **Sketch** $z(t) = r(t) + r(t-1) - 2u(t-2) - r(t-4) + r(t-8)$.
6. (4 points) Find the **energy or power**, as appropriate, of $z(t)$.
7. (6 points) Let $w(t) = 7 \sin(\omega_1 t)$. **Halve the frequency** of the signal, then **advance** it 2 seconds earlier, and then **fold it**. **Show each step** of your transformation.
8. (6 points) Let $v(t) = r(t-1) - 2r(t-2) + r(t+3)$. **Decompose $v(t)$** into even and odd signals such that $v(t) = v_e(t) + v_o(t)$.
9. (5 points) **Calculate** the **energy or power** as appropriate of $q(t) = (4+3j)e^{j\pi t/3}u(t)$.

10. (6 points) Let $x(t)$ be an unknown system input and $y(t)$ be the corresponding system output. Specifically, let $y(t) = t \times x(t-2)$. **Prove or convincingly explain** whether this system has each of the following properties:
- Linear
 - Time-invariant
 - BIBO stable
11. (6 points) Now, consider the system $y(t) = 3 x(t) + 4 x(t-1)$. **Prove or convincingly explain** whether this system has each of the following properties:
- Linear
 - Time-invariant
 - BIBO stable
12. (4 points) Which of the following properties are necessary for a system to have an impulse response?
- Causal
 - Linear
 - BIBO stable
 - Time-invariant

13. (15 points) Let a system have impulse response $h(t) = 2r(t) u(4-t)$. Let the system input be $x(t) = 3u(t) - 3u(t-4)$. **Find the system output $y(t)$ using convolution. Sketch your result.**

14. (12 points) A periodic signal has the Fourier Series $\{2j/5, 0, 2j/3, 0, -2j, \underline{5}, 2j, 0, -2j/3, 0, -2j/5\}$. $\omega_0 = 6$.

- a. What is the **DC offset** of the signal?
- b. Is the signal **even, odd, or neither**?
- c. **Sketch** the **power spectrum** of the signal.
- d. What is the **power** of the signal?
- e. What is the Fourier **transform** of this periodic signal? (Hint: Table 5.6)
- f. What is the **time-domain signal** itself?

15. (4 points) Sketch the **magnitude response** from -10 to 10 Hz of a **lowpass filter** that passes signals below 3 Hz, but blocks signals outside of this range.
16. (6 points) Determine the **impulse response $h(t)$** of this system if the **phase shift is 0**. Hint: The transfer function $H(\omega)$ is the Fourier transform of the impulse response. You will need to evaluate an integral and simplify. Hint 2: If you simplify correctly, the result will be real.
17. (6 points) Let a system have impulse response $h(t) = 5e^{-2t}u(t)$. Let the system input be the steady state signal $x(t) = \cos(6\pi t)$. What is the **output**?