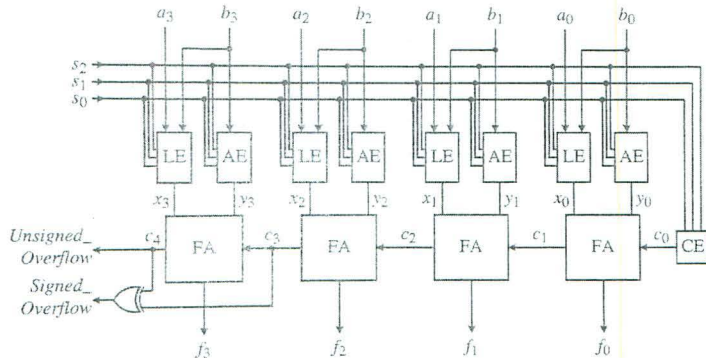


CE-1901-11 - Dr. Durant - Quiz 8  
Fall 2016, Week 9 Quiz

1. (6 points) ALUs



a. (2 points) **Complete** the following table for a 4-operation ALU (an 8-operation ALU is shown for reference):

S	Operation	Expression	LE (FA:a)	AE (FA:b)	CE (FA0:c <sub>i</sub> )
0	Decrement	--A	A	<del>0</del> 1	<del>0</del> 1
1	XOR	$A \oplus B$	$A \oplus B$	0	0
2	Subtract	$A - B$	A	$\overline{B}$	1
3	Add	$A + B$	A	B	0

b. (2 points) **Explain** why the given extender values for decrement are correct. **Provide** an example where the input  $A = 1010$ .

c. (2 points) **Design** the LE using a K-map.

(b) 
$$\begin{array}{r} 11100 \leftarrow CE \rightarrow c_0 \\ 1010 \leftarrow LE \rightarrow \text{pass } A \\ \underline{000} + 1111 \leftarrow AE \rightarrow b_i = 1 \Rightarrow B = -1 \\ \hline 1001 = 9 = 10 - 1 \checkmark \end{array}$$

(c) K-map for LE:

	ab	00	01	11	10
$\overline{S_1}S_0$	--A	0	0	1	1
$S_1\overline{S_0}$	$A \oplus B$	0	1	0	1
$S_1S_0$	$A + B$	0	0	1	1
$\overline{S_1}\overline{S_0}$	$A - B$	0	0	1	1

LE =  $\overline{S_1}S_0\overline{a}b + S_1a + \overline{S_0}a + a\overline{b}$  ← answer  

$$= \overline{S_1}S_0\overline{a}b + a(S_1 + \overline{S_0} + \overline{b})$$
  

$$= \overline{S_1}S_0\overline{a}b + a \overline{S_1}S_0b$$
 (factor  $\overline{a}$  from term 1 to reveal XOR)  

$$= a \oplus (\overline{S_1}S_0b)$$

Challenge question: Why is this answer expected given the LE column (hint: 3 rows output just A)?

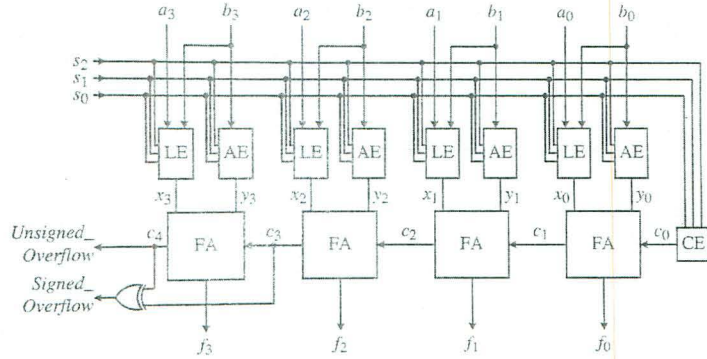
2. (4 points) In binary, multiply  $A=1010$  by  $B=1011$ , showing all 4 properly shifted intermediate products. Calculate the overall sum, showing the correct number of output bits needed to handle the largest possible product. In decimal, confirm whether your results agree with  $10 \times 11 = 110$

$$\begin{array}{r} 1010 \\ \times 1011 \\ \hline 1010 \\ 1010 \\ 0000 \\ 1010 \\ \hline 01101110 \end{array}$$

64 32    8 4 2  
└───┘    └───┘  
96      14  
└────────┘  
110 ✓

CE-1901-12 - Dr. Durant - Quiz 8  
Fall 2016, Week 9 Quiz

1. (6 points) ALUs



a. (2 points) **Complete** the following table for a 4-operation ALU (an 8-operation ALU is shown for reference):

S	Operation	Expression	LE (FA:a)	AE (FA:b)	CE (FA0:c)
0	NOR	$(A \text{ OR } B)'$	$\overline{A+B}$	0	0
1	XOR	$A \oplus B$	$A \oplus B$	0	0
2	Subtract	$A - B$	A	B'	1
3	NAND	$(AB)'$	$\overline{AB}$	0	0

b. (2 points) **Explain** why the given extender values for subtract are correct. **Provide** an example where the input  $A = 1010$  and  $B = 0111$ .

c. (2 points) **Design** the LE using a K-map.

(b)  $A - B \Rightarrow +A + \overline{B}$  2's comp. since  $-B$   
 $1 \leftarrow CE \Rightarrow c_0 = 1$   
 $1010 \leftarrow A$   
 $+ 1000 \leftarrow \overline{B}$   
 $\hline 0011 \leftarrow 3 = 10 - 7 \checkmark$

(c) K-map for LE:

	ab	00	01	11	10
s <sub>1</sub> s <sub>0</sub>	00	1	0	0	0
	01	0	1	0	1
	11	0	1	0	1
	10	0	0	1	1

$LE = \overline{s_1} \overline{s_0} \overline{a} \overline{b}$   
 $+ s_1 s_0 \overline{a}$   
 $+ s_0 \overline{a} \overline{b}$   
 $+ s_0 a \overline{b}$   
 $+ s_1 s_0 a$

add this one; there are 2 correct options

2. (4 points) In binary, multiply  $A=0110$  by  $B=1001$ , showing all 4 properly shifted intermediate products. Calculate the overall sum, showing the correct number of output bits needed to handle the largest possible product. In decimal, confirm whether your results agree with  $6 \times 9 = 45$ .

~~45~~  
54

$$\begin{array}{r} 0110 \\ \times 1001 \\ \hline 0110 \\ 0000 \\ 0000 \\ 0110 \\ \hline 00110110 \end{array}$$

32 16 42  
└──┘ └──┘  
48 6  
└────────┘ = 54 = 6 × 9 ✓